
ENHANCEMENT OF INTERSECTING ALGORITHM USING PREFIX TREE FOR TRANSACTIONS IN IDENTIFICATION OF CLOSED FREQUENT ITEM SETS IN DATA MINING

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ABSTRACT

Mining frequent itemsets is a fundamental task in data mining. Unfortunately the number of frequent itemsets describing the data is often too large to comprehend. This problem has been attacked by condensed representations of frequent itemsets that are subcollections of frequent itemsets containing only the frequent itemsets that cannot be deduced from other frequent itemsets in the subcollection, using some deduction rules. Most known frequent item set mining approaches enumerate candidate item sets, determine their support, and prune candidates that fail to reach the user-specified minimum support. Apart from this scheme we can use intersection approach for identifying frequent item set. The closed frequent item sets can be represented as the intersection of some subset of the given transactions. As the transactional database increases, the size of prefix tree also grows which make it difficult to handle. Experiments have been done to find out the efficient memory utilization of prefix tree. An improvement has been suggested to reduce the total number of branches in the prefix tree leading to reduction in its size.

Keywords: closed item set, frequent item set mining, transaction, prefix tree.

1. INTRODUCTION

Data mining is essentially the computer-assisted process of information analysis. It is often the case that large collections of data, however well structured, conceal implicit patterns of information that cannot be readily detected by conventional analysis techniques. Such information may often be usefully analyzed using a set of techniques referred to as knowledge discovery or data mining. Mining frequent itemsets is an important task in data mining.

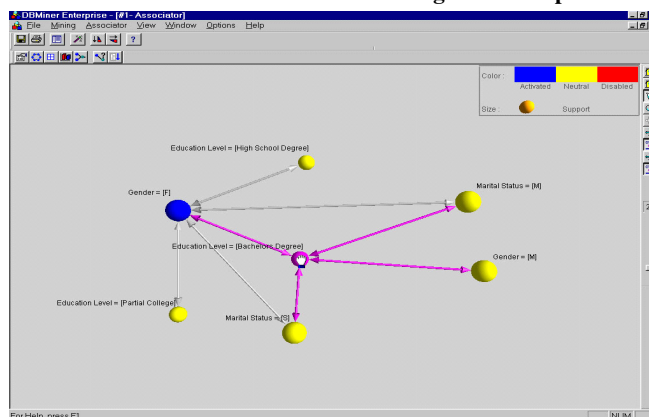
Most of the approaches enumerate candidate item sets, determine their support, and prune candidates that fail to reach the user-specified minimum support. It can be viewed as a depth-first search in the subset lattice of the item sets. However enumeration approaches worked on "top-down", since they start at the one-element item sets and work their way

downward by extending identified frequent item sets by new items. Apart from other schemes we can use intersection approach for identifying frequent item set. But the intersection approach of transaction is the least research area and need attention and improvement to be applied. The main reason why the intersection approach is less researched is that it is often not competitive with the item set enumeration approaches, at least on standard benchmark data sets. Naturally, if there are few items, there are (relatively) few candidate item sets to enumerate and thus the search space of the enumeration approaches is of manageable size. In contrast to this, the more transactions there are, the more work an intersection approach has to do, especially, since it is not linear in the number of transactions like the support computation of the item set enumeration approaches. As the transactional database increases, the size of prefix tree also grows which make it difficult to handle. Hence more time is invested in inserting new transactions and searching intersecting items. To overcome this shortcoming an attempt has been made to make the prefix tree more compact, so as to get the desired information in less time and space.

1.1 Basic Definition

1.1.1 Association rule mining: - Association rule mining [1] is a type of mining used to identify certain kind of association (interconnection relation in term of probability) among the items of database. It aims to extract interesting correlations, frequent patterns, associations or casual structures among sets of items in the transaction or other data repository.

Visualization of Association Rule Using Rule Graph



1.1.2 Support: - It specifies the fraction of transactions that contains an item sets.

1.1.3 Confidence: - It denotes the measure of trueness of the generated association rule true in probabilistic term.

1.1.4 Frequent item set: - A frequent item set is the item set whose support is greater than some user specified minimum support.

1.1.5 Closed item set: - A frequent item set is closed if there does not exist a super set that has the same support [2].

2. FREQUENT ITEM SET MINING

An important observation while mining frequent item sets is that the output is often huge and it may even exceed the size of the transaction database to mine. As a consequence, there are several approaches that try to reduce the output, if possible without any loss of in-

formation. The most basic of these approaches is to restrict the output to so-called closed or maximal frequent item sets [3]. Restricting the output of a frequent item set mining algorithm to only the closed or even only the maximal frequent item sets can sometimes reduce it by orders of magnitude. However, little information is lost: From the set of all maximal frequent item sets the set of all frequent item sets can be reconstructed, since any frequent item set has at least one maximal superset. Therefore the union of all subsets of maximal item sets is the set of all frequent item sets. Closed frequent item sets even preserve knowledge of the support values. The reason is that each frequent item set has a uniquely determined closed superset with the same support. Hence the support of a frequent item set that is not closed can be computed as the maximum of the support values of all closed frequent item sets that contain it (the maximum has to be used, because no superset can have a greater support-the so-called apriori property[4]). As a consequence, closed frequent item sets are the most popular form of compressing the result of frequent item set mining.

2.1 Basic Notions and Notation

Formally, the task of frequent item set mining can be described as follows:

B:-Base Item Set.

1. T: - (t_1, t_2, \dots, t_n) Transaction Database over an item base B.

2. $K_T(I)$:- Cover $K_T(I)$ of an item set I which is subset of B with respect to this database is set of indices of transactions that contain it. $K_T(I) = \{k \in \{1, \dots, n\} \mid I \subseteq t_k\}$

3. $S_T(I)$:- Support of an item set I which is subset of B is the size of cover.

4. We can write it as $S_T = |K_T(I)|$ That is, the number of transactions in the database T it is contained in.

5. Given a user-specified minimum support S_{min} for an item set I, an item set I is called frequent in T if and only if $S_T(I) \geq S_{min}$.

2.2 Item Set Enumeration Algorithms

A standard approach to find all frequent item sets w.r.t. a given database T and support threshold s_{min} , which is adopted by basically all frequent item set mining algorithms (except those of the Apriori family), is a depth-first search in the subset lattice of the item base B. This approach can be interpreted as a simple divide-and-conquer scheme. For some chosen item i, the problem to find all frequent item sets is split into two subproblems: (1) find all frequent item sets containing the item i and (2) find all frequent item sets not containing the item i. Each subproblem is then further divided based on another item j: find all frequent item sets containing (1.1) both items i and j, (1.2) item i, but not j, (2.1) item j, but not i, (2.2) neither item i nor j, and so on. All subproblems that occur in this divide-and-conquer recursion can be defined by a conditional transaction database and a prefix. The prefix is a set of items that has to be added to all frequent item sets that are discovered in the conditional database. Formally, all subproblems are tuples $S = (C; P)$, where C is a conditional transaction database and P is a prefix. The initial problem, with which the recursion is started, is $S = (T; \square)$, where T is the transaction database to mine and the prefix[5] is empty.

2.3 Types of Frequent Item Sets

One of the first observations one makes when mining frequent item sets is that the output is often huge-it may even exceed the size of the transaction database to mine. As a consequence, there are several approaches that try to reduce the output, if possible without any loss of information. for example:

2.3.1 Closed Item Set : A frequent item set is called closed if there does not exist a superset that has the same support, or formally

$$I \subseteq B \text{ is closed} \Leftrightarrow S_T(I) \geq S_{\min} \wedge \forall i \in B - I : S_T(I \cup \{i\}) < S_T(I) \quad \text{equation 1}$$

2.3.2 Maximal Item Set: A frequent item set is called maximal if there does not exist any superset that is frequent, or formally:

$$I \subseteq B \text{ is maximal} \Leftrightarrow S_T(I) \geq S_{\min} \wedge \forall i \in B - I : S_T(I \cup \{i\}) < S_{\min} \quad \text{equation 2}$$

From the set of all maximal frequent item sets the set of all frequent item sets can be reconstructed, since any frequent item set has at least one maximal superset. Therefore the union of all subsets of maximal item sets is the set of all frequent item sets. Closed frequent item sets even preserve knowledge of the support values. Note that closed item sets are closely related to perfect extensions: an item set is closed if it does not have a perfect extension. However, using perfect extension pruning does not mean that the output is restricted to closed item sets, because in the search not all possible extension items are considered (conditional databases do not contain all items).

3. INTERSECTING TRANSACTIONS

We discuss two ways of implementing the intersection approach: enumerating transaction sets as it is done in the Carpenter algorithm [6] and a cumulative scheme [7].

3.1 Enumerating Transaction Sets

The Carpenter algorithm [6] implements the intersection approach by enumerating sets of transactions (or, equivalently, sets of transaction indices) and intersecting them. Technically, the task to enumerate all transaction index sets is split into two sub-tasks: (1) enumerate all transaction index sets that contain the index 1 and (2) enumerate all transaction index sets that do not contain the index 1. These sub-tasks are then further divided w.r.t. the transaction index 2: enumerate all transaction index sets containing (1.1) both indices 1 and 2, (1.2) index 1, but not index 2, (2.1) index 2, but not index 1, (2.2) neither index 1 nor index 2, and so on.

3.2 Prefix Tree Implementation

The existing system specifies an intersection approach to find out the closed frequent item set. The core problem of implementing the scheme is to find a data structure for storing the closed item sets that allows us to quickly compute the intersections of these sets with a new transaction and to merge the result with them. A prefix tree implementation is used to serve this purpose. Prefix tree, is an ordered tree data structure that is used to store an associative array where the keys are usually strings. Unlike a binary search tree, no node in the tree stores the key associated with that node, instead, its position in the tree defines the key with which it is associated. All the descendants of a node have a common prefix of the string associated with that node, and the root is associated with the empty string. Values are normally not associated with every node, only with leaves and some inner nodes that correspond to keys of interest. In the example shown, keys are listed in the nodes and values below them. Each complete English word has an arbitrary integer value associated with it. A prefix tree can be seen as a deterministic finite automaton, although the symbol on each edge is often implicit in the order of the branches.

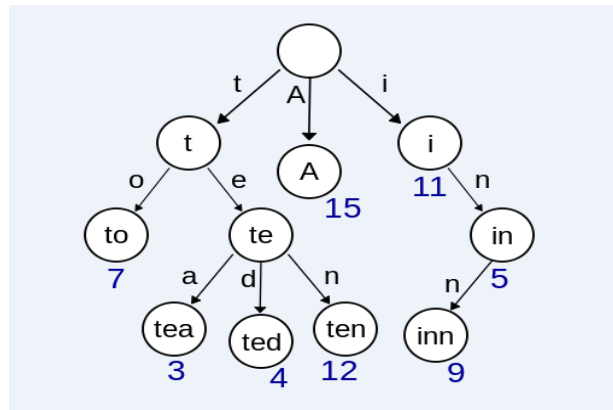


Fig-3.1 Prefix Tree

It is not necessary for keys to be explicitly stored in nodes. (In the figure, words are shown only to illustrate how the prefix tree works.)Prefix tree need not be keyed by character string. The same algorithms can easily be adapted to serve similar functions of ordered lists of any construct, e.g., permutations on a list of digits or shapes. In particular, a bitwise prefix tree is keyed on the individual bits making up a short, fixed size of bits such as an integer number or pointer to memory.

4. INTERSECTING ALGORITHM

In the intersection approach after adding the transaction to the prefix tree we need to perform the intersection of currently added transaction with all the existing transaction in the prefix tree. The proposed algorithm for performing the intersection is defined as:-

```

voidintersect (NODE_ node, NODE **ins)
{
    //intersect with transaction
    inti; // buffer for current item
    NODE *d; // to allocate new nodes
    while (node)
    {
        // traverse the sibling list
        i = node->item; // get the current item
        if (trans[i])
        {
            // if item is in intersection
            while ((d = *ins) && (d->item > i))
            ins = &d->sibling; //find the insertion position
            if (d // if an intersection node with
            && (d!item == i)) // the item already exists
            {
                if (d->step >= step) d->supp--;
                if (d->supp < node->supp)
                d->supp = node->supp;
                d->supp++; // update intersection support
                d->step = step;
            }
            // and set current update step
        }
        else
    }
}
    
```

```
{ // if there is no corresp. node
d = malloc(sizeof(NODE));
d->step = step; // create a new node and
d->item = i; // set item and support
d->supp = node->supp+1;
d->sibling = *ins;
*ins = d;
d->children = NULL;
} // insert node into the tree
if (i<= imin) return; // if beyond last item, abort
isect(node->children, &d->children);
}
else
{ // if item is not in intersection
if (i <= imin) return; // if beyond last item, abort
isect(node->children, ins);
} // intersect with subtree
node = node->sibling; // go to the next sibling
} // end of while (node)
} // isect()
```

In more detail, the procedure works as follows: whenever the item in the current sibling equals an item in the transaction (that is, whenever $trans[i]$ is true) and thus the item is in the intersection, it is checked whether the sibling list starting at $*ins$ contains a node with this item, because this node has to represent the extended intersection. If such a node exists, its support is updated. For this update the step field and variable are vital, because they allow us to determine whether the current transaction was already counted for the support in the node or not. If the value of the step field in the node equals the current step, the node has already been updated and therefore the transaction must be discounted again before taking the maximum. The maximum is taken, because we have to determine the support from the largest set of transactions containing the item set represented by the node. If a node with the intersection item does not exist, a new node is allocated and inserted into the tree at the location indicated by ins . In both cases (with the current item in the transaction or not, that is, with $trans[i]$ true or false) the sub-tree is processed recursively, unless the item of the current node is not larger than the minimum item in the current transaction. The only difference between the recursive calls is that in the case where the current item is in the intersection, the insertion position is advanced to the children of the current node.

5. EXPERIMENTS

As the transactional database increases, the size of prefix tree also grows which make it difficult to handle. Hence more time is invested in inserting new transactions and searching intersecting items. To overcome this shortcoming an attempt has been made to make the prefix tree more compact, so as to get the desired information in less time and space. An improvement has been suggested to reduce the total number of branches in the prefix tree leading to reduction in its size.

So we are suggesting the following steps for making a tree out of transaction database.

Step1:-Enumerating The Transaction Database.

	A	B	C	D	E	F	G
t1	4	0	0	3	0	0	0
t2	0	0	3	2	0	1	0
t3	3	3	0	0	0	0	1
t4	2	2	2	0	2	0	0
t5	1	1	1	1	1	0	0

Table-1 Enumerated database

Step2:-Find Out The Support Value Of Individual Item.

a =4 b=3 c=3 d=3 e=2 f=1 g=1

Step3:-Arrange The Items In Decreasing Value Of Initial Support

	A	B	C	D	E	F	G
t1	4	0	0	3	0	0	0
t2	0	0	3	2	0	1	0
t3	3	3	0	0	0	0	1
t4	2	2	2	0	2	0	0
t5	1	1	1	1	1	0	0

Table-2 Decreasing ordering of items in database

The database is already taken in increasing order of their initial support value

Step4:-Arrange The Transactions In The Increasing Size (No. Of Item Contains).

	A	B	C	D	E	F	G
t1	4	0	0	3	0	0	0
t2	0	0	3	2	0	1	0
t3	3	3	0	0	0	0	1
t4	2	2	2	0	2	0	0
t5	1	1	1	1	1	0	0

Table-3 Transaction ordering according to size

Step 5:- Make Prefix Tree Out of Transaction Database.

Step 6:- Report The Closed Item Set.

Two parameters have been taken for measuring the prefix tree size and its memory utilization.

(A).Total Number Of Nodes InThe Prefix Tree.

(B).Total Number Of Paths Existing In The Prefix Tree.

6. RESULTS

```

there is total 5 transactions and 7 number of itens.
4 3 0 0 0 0 0
3 0 0 3 0 1 0
0 2 3 0 0 0 1
2 0 2 2 2 0 0
1 1 1 1 1 0 0
    
```

Fig -5.1. Enumerate the transaction database

```

symbol list :a support = 4
symbol list :d support = 3
symbol list :c support = 3
symbol list :b support = 3
symbol list :e support = 2
symbol list :g support = 1
symbol list :f support = 1
there is total 5 transactions and 7 number of itens.
4 3 0 0 0 0 0
3 0 0 3 0 1 0
0 2 3 0 0 0 1
2 0 2 2 2 0 0
1 1 1 1 1 0 0
    
```

Fig- 5.2. Find out the initial support value of each item in the transaction database

```

G:\rashmi\programs\one\two.exe
transaction1 has size 2 and counter is 1 and transcation is as :ad
transaction2 has size 3 and counter is 1 and transcation is as :abg
transaction3 has size 3 and counter is 1 and transcation is as :cdf
transaction4 has size 4 and counter is 1 and transcation is as :ahce
transaction5 has size 5 and counter is 1 and transcation is as :ahcde
symbol list :a support = 4
symbol list :d support = 3
symbol list :c support = 3
symbol list :b support = 3
symbol list :e support = 2
symbol list :g support = 1
symbol list :f support = 1
there is total 5 transactions and 7 number of itens.
4 3 0 0 0 0 0
3 0 0 3 0 1 0
0 2 3 0 0 0 1
2 0 2 2 2 0 0
1 1 1 1 1 0 0
    
```

Fig-5.3. Arrange the items according to decreasing initial support value.


```

transaction1 has size 2 and counter is 1 and transcation is as :ad
transaction2 has size 3 and counter is 1 and transcation is as :abg
transaction3 has size 3 and counter is 1 and transcation is as :cdf
transaction4 has size 4 and counter is 1 and transcation is as :abce
transaction5 has size 5 and counter is 1 and transcation is as :abcde
symbol list :a support = 4
symbol list :d support = 3
symbol list :c support = 3
symbol list :b support = 3
symbol list :e support = 2
symbol list :g support = 1
symbol list :f support = 1
there is total 5 transactions and 7 number of itans.
4      3      0      0      0      0      0
3      0      0      3      0      1      0
0      2      3      0      0      0      1
2      0      2      2      2      0      0
1      1      1      1      1      0      0
    
```

Fig-5.4. Arrange the transaction according to increasing size

```

Adding t1 to prefix tree
a-1d-1

Adding t2 to prefix tree
a-1d-1
a-1b-1g-1

intersection of abg and ad contains intersecting items are as:a
a-2d-1
a-1b-1g-1

Adding t3 to prefix tree
a-2d-1
a-1b-1g-1
c-1d-1f-1
    
```

Fig- 5.5. Make the prefix tree out of the transaction database

```

intersection of cdf and ad contains intersecting itens are as:d
a-2d-1
a-1b-1g-1
c-1d-1f-1
d-2

intersection of cdf and abg contains empty list
a-2d-1
a-1b-1g-1
c-1d-1f-1
d-2

Adding t4 to prefix tree
a-2d-1
a-1b-1g-1
c-1d-1f-1
d-2
a-1b-1c-1e-1
    
```

Fig- 5.6. Intermediate tree structure

```

intersection of abce and ad contains intersecting itens are as:a
a-3d-1
a-1b-1g-1
c-1d-1f-1
d-2
a-1b-1c-1e-1

intersection of abce and abg contains intersecting itens are as:ab
a-3d-1
a-2b-2g-1
c-1d-1f-1
d-2
a-1b-1c-1e-1

intersection of abce and cdf contains intersecting itens are as:c
a-3d-1
a-2b-2g-1
c-2d-1f-1
d-2
a-1b-1c-1e-1
    
```

Fig-5.7. Intermediate tree structure

```

Adding t5 to prefix tree
a-3d-1
a-2b-2g-1
c-2d-1f-1
d-2
a-1b-1c-1e-1
a-1b-1c-1d-1e-1

intersection of abcde and ad contains intersecting itens are as:ad
a-4d-2
a-2b-2g-1
c-2d-1f-1
d-2
a-1b-1c-1e-1
a-1b-1c-1d-1e-1

intersection of abcde and abg contains intersecting itens are as:ab
a-4d-2
a-3b-3g-1
c-2d-1f-1
d-2
a-1b-1c-1e-1
a-1b-1c-1d-1e-1

intersection of abcde and cdf contains intersecting itens are as:cd
a-4d-2
a-3b-3g-1
c-3d-2f-1
d-2
a-1b-1c-1e-1
a-1b-1c-1d-1e-1
    
```

Fig-5.8. Intermediate tree structure

```

intersection of abcde and abce contains intersecting itens are as:abce
a-4d-2
a-3b-3g-1
c-3d-2f-1
d-2
a-2b-2c-2e-2
a-1b-1c-1d-1e-1

There are total 18 nodes in the tree.
There is 6 number of paths.
    
```

Fig-5.9. Final prefix tree

7. CONCLUSIONS

The study and experiments conducted of intersection approach shows that this approach outperforms most of the existing technology in different database. The core of intersection approach is the prefix data structure that is used to represent the transaction database along with the intersecting item that are also represent in the nodes of prefix tree. The main problem that is associated with this data structure is that the size of the prefix tree. The size of prefix tree grows very large when we process larger number of transaction. Smaller prefix tree take less time in searching for any particular node and also makes its handling easier. The main fact behind the reduction in size is that items with higher initial support value have more probability of occurring in intersection. Arranging of items within the transaction has effect on the size of prefix tree. Arranging the items in decreasing order of support value allow the higher support item to exists at the first level in prefix tree. These higher support items exist more often in intersection and while we search for intersecting items in the tree they can be found at first level of prefix tree thus it prevents extra branches to be added in the tree and thus the number of branches in the prefix tree reduces. Hence we conclude that arranging the items according to decreasing initial support value reduces the size of prefix tree. It considerably reduces the total number of branches and nodes in the prefix tree and the effect of this reduction reflect in the total memory utilization of the prefix tree.

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